Prediction of a two-dimensional high-\(T_C\) f-electron ferromagnetic semiconductor

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Two-dimensional (2D) ferromagnetic semiconductors (FMSs) exhibit novel spin-dependent electronic and optical properties, opening up exciting opportunities for nanoscale spintronic devices. However, experimentally confirmed 2D FMSs based on transition metal ions are rather limited and their performances are not satisfactory, e.g. typically with low Curie temperatures and small magnetic signals. Different from most known 2D magnets based on d-electrons, here an exotic 2D FMS based on rare-earth ions with f-electrons, a GdI\(_2\) monolayer, is predicted to have a large magnetization (8 \(\mu_B\) f.u. \(^{-1}\)), whose ferromagnetism can survive near room temperature (241 K).

In addition, with a small exfoliation energy from its layered van der Waals (vdW) bulk, this GdI\(_2\) monolayer holds excellent dynamical and thermal stabilities, making our prediction promising in experiments. Our prediction not only offers a compelling FMS for spintronics, but also provides an alternative route to acquire more high-performance 2D FMSs, going beyond pure d-electron compounds.

Spintronic devices, making use of both charge and spin, have generated world-wide interest due to their faster information operation, lower energy consumption, and higher storage density compared to conventional charge-based electronics.\(^1\)\(^-\)\(^4\) One branch of the most promising candidates for spintronics is ferromagnetic semiconductors (FMSs), which have the advantages of combining conventional semiconductor electronics and non-volatile magnetic storage at finite temperature.\(^3\) FMSs can be used for spin injection, generation, manipulation, and detection, which can be easily implemented in devices by applying nowadays well-developed semiconductor technology.\(^5\) Unfortunately, due to the incompatibility between ferromagnetism and semiconductivity, intrinsic FMSs are rare in nature and their Curie temperatures (\(T_C\)) are usually much lower than room temperature, greatly hindering their practical application.\(^7\) Although dilute magnetic semiconductors, which produce ferromagnetism by doping with magnetic elements, were thought to possess potential high-temperature \(T_C\), their reproducible \(T_C\) values are still limited below 200 K (e.g., 155 K for the most successful Mn-doped GaAs).\(^8\) Besides, problems such as low spin polarization, low dopant solubility, phase separation, bad controllability, and formation of ferromagnetic (FM) clusters

New concepts

Two-dimensional (2D) spintronics with the goal of achieving room-temperature Curie temperature (\(T_C\)) ferromagnetism with large spin polarization, especially ferromagnetic semiconductors (FMSs), are key to the development and application of spintronic devices. However, the currently demonstrated 2D FMSs suffer from rather low Curie temperatures and the magnetic exchange mechanism is unclear. In this work, reported for the first time, a high Curie temperature 2D FMS of rare-earth halides (GdI\(_2\) monolayer) is achieved with a number of desirable magnetic properties such as near-room-temperature \(T_C\), large magnetization, sizable MAE, and good bipolar magnetic conductivity. Most interestingly, a new magnetic coupling mechanism in the 2D regime, namely, a d-electron-mediated f-f coupling mechanism, has been proposed. This intriguing magnetism originated from the coexistence of effective f-f direct-exchange (Gd\(_{\text{Ir}}\)-Gd\(_{\text{Ir}}\)) and super-exchange (Gd\(_{\text{Ir}}\)-Gd\(_{\text{Ir}}\)-Gd\(_{\text{Ir}}\)) interactions. Meanwhile, this monolayer possesses excellent thermal, dynamical, and mechanical stabilities and it has great feasibility of experimental exfoliation from its layered bulk. Our work provides a very promising way to realize a 2D intrinsic room temperature FMS, and will certainly boost the study of 2D rare-earth magnetism.

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appear difficult to solve.\textsuperscript{3,5} After many years of studies on dilute magnetic semiconductors, the origin of ferromagnetism in these systems remains a subject of debate.\textsuperscript{7–9} “Is it possible to create magnetic semiconductors that work at room temperature?” is still one of the most challenging 125 big questions in science in this century.\textsuperscript{10}

The rise of 2D magnetism is expected to have a transformative effect on spintronics applications, such as high integration density and high operation data-processing speed.\textsuperscript{11–14} For example, the recent discovery of 2D FMSs, including the CrX\textsubscript{3} (X = Cl, Br, I) monolayer\textsuperscript{15,16} and Cr\textsubscript{2}Ge\textsubscript{2}Te\textsubscript{6} bilayer,\textsuperscript{17} provides a new playground for applications of 2D spintronics at the nanoscale. Besides these synthesized FMSs, other 2D FMSs have also been predicted based on first-principles calculations, such as CrSBr.\textsuperscript{18–38} Unfortunately, the $T_C$ values of these FMSs are still much below room temperature, although their $T_C$ values could be moderately increased by carrier doping,\textsuperscript{39–41} strain,\textsuperscript{25,42,43} and electric fields.\textsuperscript{12,44} Three FMSs were recently predicted to be room-temperature ones;\textsuperscript{20,45,46} however their corresponding layered vdW bulk crystals are absent.

Rare-earth elements, which typically have large magnetic moments and high magnetocrystalline anisotropy, are very important in both fundamental scientific research as well as real applications of high performance magnets.\textsuperscript{47–49} However, due to the highly localized characteristic of 4f electrons, the direct overlap of 4f orbitals between neighbor rare-earth elements, as well as the hybridization between 4f orbitals and p orbitals of neighbor anions, is mostly negligible. As a result, the direct exchange and superexchange mediated by anions are usually very weak between rare-earth magnetic elements, which is the most serious drawback in the pursuit of high-temperature 4f magnetism. Therefore, the 4f rare-earth elements seem to be ineffective in the pursuit of high-$T_C$ 2D FMSs, and thus no study of 2D 4f magnets has been reported, at least to our best knowledge.

In this work, unexpectedly, we demonstrate the feasibility to realize a promising high-$T_C$ FMS of 2D rare-earth halides (GdI\textsubscript{2} monolayer). The unique exception comes from the coexistence of spin polarized 5d orbitals and 4f orbitals in Gd\textsuperscript{2+}. The combination of strong Gd\textsuperscript{4f}–Gd\textsuperscript{5d} interactions within each Gd\textsuperscript{2+} ion and strong Gd\textsuperscript{5d}–I\textsuperscript{5p}–Gd\textsuperscript{5d} interactions leads to strong ferromagnetism in the 2D limit, i.e. high-$T_C$ ($\sim 241$ K), large magnetization ($\sim 8$ $\mu_B$ f.u.\textsuperscript{–1}), and large magnetic anisotropy energy ($\sim 553$ $\mu$eV Gd\textsuperscript{–1}). This work not only takes advantage of the properties of rare-earth elements with large magnetic moment, but also overcomes the weakness of localized f orbital magnetic exchange in 2D magnetism.

The reason we choose the GdI\textsubscript{2} monolayer is as follows. Among all rare-earth elements, Gd is the only room-temperature ferromagnetic rare-earth metal, and some of its compounds also possess high Curie temperatures, such as 352 K for GdScSi.\textsuperscript{50} The FM GdI\textsubscript{2} bulk has also been first synthesized by Mee and Corbett\textsuperscript{51} with room-temperature $T_C$ (300–340 K).\textsuperscript{52–54} In the FM GdI\textsubscript{2} bulk, each Gd ion is caged within an I\textsubscript{6} trigonal prism (Fig. 1a). It has a layered vdW 2H-MoS\textsubscript{2}-type structure, in which the I–Gd–I sandwich layers are stacked together along the c-axis.

![Fig. 1](a) Top and side views of the GdI\textsubscript{2} monolayer. (b) Calculated exfoliation energy vs. separation distance ($d$–$d_0$), where $d_0$ indicates the vdW gap between adjacent layers in the bulk crystal. (c) Evolution of the total energy from AIMD simulations and the inset is the structure of the GdI\textsubscript{2} monolayer at the end of the AIMD simulation after 10 ps. (d) Phonon dispersion of the GdI\textsubscript{2} monolayer.
in an AB stacking sequence (Fig. S1a, ESI†). The electron localization function (Fig. S1b, ESI†) confirms that GdI₂ is made up of weak vDW bonded 1-Gd-I units, which makes it possible for a GdI₂ monolayer to be exfoliated from its layered bulk. Meanwhile, the interlayer FM coupling should be very weak due to the relatively large distance between two interlayer nearest-neighbor Gd atoms (7.84 Å, Fig. S1, ESI†). This weak interlayer interaction also makes it possible for this monolayer to maintain the room-temperature $T_c$ of the FM bulk crystal.

To explore the possibility of exfoliation of a GdI₂ monolayer from its layered bulk crystal, we calculate the cleavage energy from a 4-layer slab. As shown in Fig. 1b, the energy increases with increasing separation distance ($d-d_0$), and converges to 0.26 J m⁻², which is notably less than the experimental value of graphite (0.36 J m⁻²),55 suggesting the experimental feasibility. Fig. 1c shows the corresponding fluctuations of the total potential energies for the GdI₂ monolayer during the ab initio molecular dynamics (AIMD) simulations and the snapshots of the geometries after annealing at 300 K for 10 ps. The small fluctuations of the energy and integrity of the original configuration with time evolution confirm its good thermal stability. The absence of imaginary modes in the whole Brillouin zone establishes the dynamic stability of the GdI₂ monolayer as well (Fig. 1d). Besides, the GdI₂ monolayer also meets the mechanical stability Born criteria,56 and it has good in-plane stiffness (ESI†). The small cleavage energy and good stabilities strongly support that the 2D GdI₂ monolayer could possibly be prepared in experiment and survive at room temperature.

The excellent stability and large feasibility of experimental exfoliation of the GdI₂ monolayer inspire us to explore its magnetic and electronic properties. The 2 × 2 supercell of the GdI₂ monolayer with various magnetic orders as schematically shown in Fig. S2 (ESI†) is considered to determine the magnetic ground state. Our calculations show that the GdI₂ monolayer has a FM ground state with an energy difference between the FM and AFM states of 139 meV Gd⁻¹. The spin density presented in Fig. S2 (ESI†) indicates that the ferromagnetism mainly comes from the contribution of the Gd ion. Spin-polarized DFT calculations using different exchange–correlation functionals show that the GdI₂ monolayer is a semiconductor with an indirect band gap of 0.62 eV (PBE + U) and 1.21 eV (HSE06) (Fig. 2a and b). Note that the HSE06 and PBE + U functionals produce quite similar band structures except for the size of the band gap. The spin–orbit coupling (SOC) effect is also considered and it only decreases the band gap a little bit (Fig. S3, ESI†). Detailed analysis of different atomic components reveals that the conduction and valence bands near the Fermi level are dominated by the Gd atom (Fig. 2). Very interestingly, the GdI₂ monolayer shows a typical bipolar magnetic semiconductor (BMS) feature,57 in which the valence and conduction bands possess opposite spin-polarization orientation when approaching the Fermi level. Simply by adjusting the position of the Fermi level, the unique electronic structure in the BMS enables the feasibility to achieve half-metallicity, which can provide 100% spin-polarized current.58–60 Clearly, completely spin-polarized currents with reversible spin polarization can be created and controlled by applying a gate voltage, which can be easily applied locally in contrast to magnetic fields.

The calculated spin-polarized atom-projected and orbital-projected density of states (Fig. 2c and Fig. S4, ESI†) further reveals that the magnetism in the GdI₂ monolayer is mainly contributed by both 4f and 5d orbitals of Gd atoms. All spin-up 4f orbitals are occupied while the spin-down ones remain empty (Fig. S4, ESI†). The narrow and high peaks in the DOS plot indicate that the 4f electrons of Gd are highly localized. Meanwhile, the 5d orbitals are also split into the lower and upper manifolds, which are separated by about 1 eV near the Fermi level. The chemical bonding makes the completely occupied 5p orbitals mainly centered at ~ 4 eV below the Fermi level, which are barely affected by the 4f states. Fig. 2c shows that the top of the valence band is primarily attributed to Gd 5d states, hybridized weakly with 1 5p states.

Because the 4f orbitals on Gd atoms are highly localized, their direct participation in magnetic exchange coupling should be negligible. In order to understand the nature of FM coupling in the GdI₂ monolayer, intra- and inter-atomic interactions need to be considered. For the intratomic interactions, the wave function of 5d electrons is more extended than that of 4f electrons. Meanwhile, the intratomic Hund interactions between 4f and 5d electrons are strong. As a result, the 5d electrons are spin-polarized in the vicinity of the Fermi level (Fig. 2c) and the 4f moments will align in a cooperative fashion via the surrounding polarized 5d electrons, resulting in intrinsic large magnetic moments.61 For the interatomic coupling, the ferromagnetic order can be determined by the coexistence of the direct- and super-exchange interactions. On one hand, the trigonal prismatic crystal field splits 5d orbitals into three groups, a (dₓ²−z², e₁ (dₓz, dᵧz)), and e₂ (dₓz, dᵧz) (Fig. 3a).
Then one 5d electron will occupy the spin-up channel in the lowest-energy singlet $d_{z^2}$, making the GdI$_2$ monolayer a magnetic semiconductor. In light of Kramers' mechanism, the partially occupied states will lead to the FM direct-exchange interaction [Gd$_{5d}$–Gd$_{5d}$] between the nearest neighboring Gd spins. On the other hand, the bond angle of Gd$_{5d}$–I$_{5p}$–Gd$_{5d}$, $\theta$ ($\sim 82.2^\circ$), is close to $90^\circ$, which also prefers FM coupling according to the Goodenough–Kanamori–Anderson (GKA) rules.62–64 The schematic of the Gd–I–Gd super-exchange interaction mediated by I anions is plotted in Fig. 3b, which arises from the p–d hybridization between I 5p and Gd 5d orbitals. As a result, the effective 4f–4f interaction is FM, mediated by the 5d–(5p)–5d exchanges.

Magnetic anisotropy is an important requirement for realizing long-range ferromagnetic ordering.65 Magnetic anisotropy can be scaled by the MAE, which directly correlates with the thermal stability of magnetic data storage. Calculations of total energies including SOC are therefore performed on the GdI$_2$ monolayer to estimate the MAE along the $x$ (100), $y$ (010), and $z$ (001) directions as summarized in Table S1 (ESI†). As a result, this monolayer maybe exhibits an easy magnetic $xy$ plane. The angular dependence of the MAE is presented in Fig. 4a, which clearly shows that the MAE strongly depends on the direction of magnetization in the $xz$ and $yz$ planes, whereas the MAE is isotropic in the $xy$ plane. As a result, we observe a strong dependence of the MAE on the out-of-plane angle of magnetization, similar to that for the VS$_2$ and FeCl$_2$ monolayers,66,67 and in contrast to the easy axis for the Fe$_7$GeTe$_2$68 and CrI$_3$15 monolayers. The strong magnetic anisotropy in this monolayer is further confirmed as shown in Fig. 4b, in which the corresponding MAE through the whole space is displayed. The MAE is zero in plane and reaches a maximum of 553 $\mu$eV Gd$^{-1}$ perpendicular to the plane, which is comparable to that of the CrI$_3$ monolayer (685 $\mu$eV Cr$^{-1}$) and larger than those of CrXTe$_3$ (X = Si, Ge, Sn) monolayers (209, 110, 69 $\mu$eV Cr$^{-1}$).29

$T_C$ is another key parameter for the practical application of spintronic devices. Monte Carlo (MC) simulations with the Heisenberg model were performed to estimate the $T_C$ of the GdI$_2$ monolayer. The spin Hamiltonian is defined as

$$H = -J \sum_{i,j} S_i \cdot S_j - A (S_i^z)^2$$

Fig. 3 (a) Trigonal prism of six I ions surrounding the Gd ion. (b and c) Schematics of the Gd–I–Gd superexchange path via d–p–d orbitals with the nearest Gd–Gd distance $d_1$, Gd–I distance $d_2$, and Gd–I–Gd bond angle $\theta$.

Fig. 4 Angular dependence of the magnetic anisotropic energy (MAE) of the GdI$_2$ monolayer with the direction of magnetization lying on three different planes (a) and the whole space (b). The magnetic moment $M$ (red), specific heat $C_v$ (blue), and magnetic susceptibility $\chi$ (green) as functions of temperature for the GdI$_2$ monolayer (c).
where $J$ is the nearest neighbor exchange parameter, $S$ is the spin vector of each atom, and $A$ is an anisotropy energy parameter (more details can be found in our previous work\textsuperscript{27,40,60}). A large $50 \times 50$ supercell is used. Using the energy difference between AFM and FM (139 meV Gd\textsuperscript{2+}) and normalized $S (|S| = 1)$, the estimated Heisenberg exchange parameter $J$ is 34.79 meV from $\Delta E = E_{\text{AFM}} - E_{\text{FM}} = 4J$. After the system reaches equilibrium at a given temperature, the specific heat capacity $C_v$ is calculated by $C_v = \frac{1}{k_B T^2} < (E^2) - <E>^2 >$. Given the exact solution to the spin Hamiltonian, $T_C$ can be estimated from the peak positions of specific heat $C_v$ or magnetic susceptibility $\chi$. The calculated magnetic moment $M$ and semiconducting behavior enables the GdI\textsubscript{2} monolayer to be a promising candidate for spintronic applications.

As we point out above, the synergetic effect of direct- and super-exchange interactions determines the magnetic ground state of the GdI\textsubscript{2} monolayer. The distance $d_1$ and angle $\theta$ play an important role in this exchange mechanism. Besides, the intrinsic physical properties would be also affected by the substrate due to the lattice-mismatch-induced strain in the experimental process. Therefore, it is desirable to investigate the effect of the strain and carrier doping on the magnetic behavior. Fig. 5a and c show the curves of $\Delta E$, $d_1$, and $\theta$ under the compression and tension strain. $\Delta E$ decreases slightly while $d_1$ and $\theta$ increase as the strain is increased. The increased $d_1$ weakens the direct exchange while the increased angle $\theta$ (from 82.2° to 85.1°) enhances the super-exchange interaction according to the GKA rule.\textsuperscript{72} For the compressive strain, however, $\Delta E$ increases while $d_1$ and $\theta$ decrease as the strain is increased. The decreased $d_1$ makes the direct exchange become more important in determining the FM ordering. On the other hand, the bond angle $\theta$ of Gd–I–Gd increases monotonically as well and deviates from 90°, and thus the super-exchange interaction becomes weak. Importantly, in the range of strain investigated, the near room-temperature $T_C$ and the BMS characteristic of the GdI\textsubscript{2} monolayer are well preserved (Fig. S8 and S9, ESI†, respectively). The stabilities and possible phase transformation of the GdI\textsubscript{2} monolayer under strain are also discussed (Fig. S10, ESI†). For carrier doping, $\Delta E$ changes slightly when the hole concentration increases, while it gradually decreases when the electron concentration increases (Fig. 5b). Meanwhile, $d_1$ and the angle $\theta$ increase with increasing electron or hole concentration (Fig. 5d). With increasing carrier doping concentration, the GdI\textsubscript{2} monolayer undergoes a BMS to half-metal transition (Fig. S11, ESI†). Meanwhile, in the range of hole doping, the near room-temperature $T_C$ of the GdI\textsubscript{2} monolayer is also well preserved (Fig. S12, ESI†), while $T_C$ decreases a little with increasing electron doping (Fig. S13, ESI†).

In summary, we have demonstrated a promising way to achieve a 2D FMS by a d-electron-mediated f–f magnetic coupling

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**Fig. 5** (a) Strain and (b) carrier dependence of the exchange energy $\Delta E = E_{\text{AFM}} - E_{\text{FM}}$ per unit cell for the GdI\textsubscript{2} monolayer. The nearest Gd–Gd distance $d_1$ and Gd–I–Gd bond angle $\theta$ as a function of strain (c) and carrier doping (d).
mechanism. Owing to the effective f-f exchange interactions, a promising 2D intrinsic FMS with near room-temperature $T_C$ (241 K) was predicted as realized in the GdI$_2$ monolayer by using first-principles calculations. The FM states, semiconductivity, and the near-room-temperature $T_C$ can be well maintained under strain conditions. Meanwhile, the GdI$_2$ monolayer possesses BMS properties and provides completely spin-polarized currents with reversible spin-polarization simply by applying a gate voltage. Considering the excellent dynamical and thermal stability, and the fact that its cleavage energy is even smaller than that of graphene, the GdI$_2$ monolayer could be fabricated by mechanical cleavage like graphene. However, we have to point out that the nature of magnetism in a monolayer with an easy magnetic $xy$ plane still remains an open question, as 2D xy magnetism is not expected to show long-range order at finite temperature. Considering the fact that two-dimensional materials are usually synthesized on a substrate, a suitable substrate (such as in heterointerface engineering) might facilitate the synthesis of a GdI$_2$ monolayer, although it is still very challenging, in the future. Our findings not only provide new insights into the magnetic exchange in rare-earth halides at the nanoscale, but also give opportunities for future spintronic investigations and applications.

**Method**

All the calculations were performed based on spin-polarized density functional theory (DFT) with the Perdew–Burke–Ernzerhof (PBE) functional in the generalized gradient approximation (GGA) as implemented in the Vienna $ab$ initio simulation package (VASP). The projector-augmented plane wave (PAW) approach was used to represent the ion–electron interaction, and the plane-wave cutoff energy was set to 500 eV. Structures were fully relaxed until the force and the energy were converged to 0.01 eV Å$^{-1}$ and $10^{-6}$ eV, respectively. The standard pseudo-potential for Gd containing 18 electrons was used, and the 5s$^2$5p$^6$4f$^7$5d$^1$6s$^2$ valence-electron configuration was considered. Spin–orbit coupling (SOC) has been included in the calculations because of heavy elements. Specific parameters of $U = 9.2$ eV and $J = 1.2$ eV were used for the Gd 4f orbitals, which were adopted from previous work and successfully reproduce the experimental magnetic moment of Gd ions in bulk GdI$_2$. A detailed test on $U_{eff}$ ($U_{eff} = U - J$) can be found in Fig. S14 (ESI†). The HSE06 hybrid functional was also employed to obtain a more accurate band structure and verifies the GGA + U method. We have to point out that, in most cases, the electronic and magnetic properties of 4f electron systems are hard to treat due to the strong correlation and strong spin–orbit coupling of very localized f bands. However, Gd$^{2+}$ as studied in our work is an exception, whose 4f orbitals are half-filled, i.e. 4f$^7$. Such half-filled 4f bands are simple in physics and can be well-treated from first principles. The comparison between FM and AFM states is added as shown in Fig. S15 (ESI†). Spin–orbit coupling was included to get the MAE calculation. Phonon dispersions were calculated by density functional perturbation theory embedded in the Phonopy software. AIMD simulations in the $NVT$ ensemble using the Nosé–Hoover thermostat lasted for 10 ps with a time step of 1.0 fs.$^{51}$

**Conflicts of interest**

The authors declare no competing financial interest.

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