Antiferromagnetism of Double Molybdate LiFe(MoO$_4$)$_2$

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I. INTRODUCTION

Double tungstates and molybdates with the chemical formula AB$^{3+}$(MO$_4$)$_2$ form a big family of transition metal oxides, where A is an alkali metal; B is a trivalent cation such as Bi$^{3+}$, In$^{3+}$, or Fe$^{3+}$ or a rare earth, Sm$^{3+}$ or Eu$^{3+}$; and M represents W$^{6+}$ or Mo$^{6+}$. The combinations of three categories of metal ions make this family full of varieties in physics and functionality. The inclusion of the Li ion at A site makes them suitable to be used in lithium-ion batteries as anode materials, while the W/Mo can provide a relative large spin−orbit coupling considering its 4d/5d orbitals.1,6,9 Most importantly, the B-site ions with narrow bands can provide other applicable physical properties, such as magnetism and luminescence.10−15

Recently, NaFe(WO$_4$)$_2$ was reported to exhibit an incommensurate spiral spin order at low temperature (<4 K),16 although this magnetism cannot induce a net ferroelectric (FE) polarization (P) due to the opposite chirality coexisting in this material. Differently, Liu et al. revealed a more interesting magnetic spiral in LiFe(WO$_4$)$_2$, which breaks the spatial reversal symmetry and induces a net FE P along the [010] axis below 19.7 K through the inverse Dzyaloshinskii−Moriya (DM) interaction.17 Thus, LiFe(WO$_4$)$_2$ is the second experimentally confirmed multiferroic material in the tungstate family, following the first one MnWO$_4$.18,19 Despite the common chemical formula, the crystalline structures of double tungstates/molybdates can vary in a large range. In fact, LiFe(WO$_4$)$_2$ and NaFe(WO$_4$)$_2$ are different in their space groups (C2/c vs P2/m), and the arrangements of Fe ions are distinct. Such structural diversity makes it possible to find more exotic magnetic properties in double tungstates/molybdates. For instance, it was reported that RbFe(MoO$_4$)$_2$ possesses a noncollinear magnetic order below 3.8 K which can trigger the ferroelectricity.20 In addition, there are lots of other tungstates/molybdates members, e.g., FeWO$_4$, CoWO$_4$, NiWO$_4$, CuWO$_4$, α-FeMoO$_4$, α-CoMoO$_4$, and NaCr(WO$_4$)$_2$, all of which display collinear antiferromagnetic orders and thus are not ferroelectric.21−25 Recently, Chen et al. synthesized LiFe(MoO$_4$)$_2$ and investigated it for its applications in lithium-ion batteries.6 Distinct from either LiFe(WO$_4$)$_2$ or NaFe(WO$_4$)$_2$, LiFe(MoO$_4$)$_2$ possesses a new space group P1 and another type of Fe framework. Its excellent electrochemical properties have been carefully studied. Nevertheless, its magnetic properties have never been studied yet.

In this work, we will report the magnetism of LiFe(MoO$_4$)$_2$ determined from combined studies of heat capacity, magnetic susceptibility, neutron powder diffraction, as well as density functional theory (DFT) calculation. An antiferromagnetic (AFM) phase transition is found around 23.8 K. Below the Néel temperature (T$_N$), a long-range magnetic ordering is established with a commensurate propagation vector (0, 0.5, 0) which does not yield multiferroicity. Above T$_N$, short-range magnetic correlation persists, leading to considerable magnetic entropy.
II. METHODS

High-quality polycrystalline LiFe(MoO4)2 samples were synthesized using the conventional solid state reaction method in air, with the highly purified powder of oxides and carbonates as starting materials. The stoichiometric mixtures were ground and fired at 550 °C for 24 h in air. The resultant powder was reground and pelletized under a pressure of 1000 psi into disks of 2.0 cm in diameter, and then, these pellets were sintered at 650 °C for 24 h in air again. Phase purity of the sample was checked using X-ray diffraction (XRD) with the Cu Kα radiation at room temperature. The magnetic properties were measured using a superconducting quantum interference device magnetometer (SQUID) equipped on a quantum design magnetometer (MPMSXL-7). The specific heat was measured on the physical property measurement system (PPMS, Quantum Design) using the heat relaxation method. Neutron powder diffraction (NPD) patterns were collected with neutron wavelength λ = 2.41 Å at the HB-2A powder diffractometer at the High Flux Isotope Reactor, Oak Ridge National Laboratory.

DFT calculations were performed using the Vienna ab initio simulation package (VASP) with the projector augmented-wave (PAW) potentials.26−28 The Perdew−Burke−Emzerhof for solids (PBEsol) exchange function has been adopted29 to obtain an accurate description of the crystal structure of LiFe(MoO4)2. The Hubbard U_eff (= U − J) was imposed on Fe’s d orbitals using the Dudarev implementation30 considering the strong correlation effect of 3d orbitals. No U_eff is applied to Mo’s 4d orbitals considering its empty d orbitals. The cutoff energy of the plane wave basis was fixed to 650 eV due to a quite high convergent value of Li. The Brillouin zone was adopted using 6 × 6 × 3 Monkhorst−Pack k-point mesh for the minimal magnetic unit cell. Besides, both the lattice constants and atomic positions were fully relaxed until the Hellmann−Feynman force on each atom is below 0.01 eV/Å.

III. RESULTS AND DISCUSSION

Figure 1a shows the crystal structure of LiFe(MoO4)2, which is described in the triclinic space group P1̅ (No. 2) and consisted of separated layers of [LiO2] monocapped trigonal bipyramids, [FeO6] octahedra, and [MoO4] tetrahedra. The framework of magnetic Fe ions in LiFe(MoO4)2 is shown in Figure 1b.

Figure 1c shows the powder XRD pattern of LiFe(MoO4)2 at room temperature. The lattice parameters were refined using the space group P1̅ with the Rietveld refinement technique. No impurity phase is observed in the XRD pattern. The refined lattice parameters of LiFe(MoO4)2 are a = 6.7766 Å, b = 7.1679 Å, c = 7.3104 Å, α = 90.89°, β = 110.38°, and γ = 105.21°, which are in good consistency with previous works.31,32

Besides XRD, NPD data of LiFe(MoO4)2 were collected at T = 40 K, as shown in Figure 1d. The nuclear structure refinement was conducted using FullProf with the Rietveld method.26 Our refinement confirms that the compound possesses a triclinic structure with the space group P1̅. No impurity phase was detected. The corresponding lattice parameters are a = 6.751(1) Å, b = 7.203(2) Å, c = 7.1702(1) Å, α = 90.6739(17)°, β = 110.2274(14)°, and γ = 105.5793(17)°, in agreement with above XRD results. Table 1 summarizes more parameters such as atomic coordinates and displacement parameters.

Table 1. Refined Structural Parameters of LiFe(MoO4)2 from Neutron Powder Diffraction Data Collected at 40 K with the Neutron Wavelength of λ = 2.41 Å

<table>
<thead>
<tr>
<th>atom (Wyck.)</th>
<th>x</th>
<th>y</th>
<th>z</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mo1 (2i)</td>
<td>0.3326(4)</td>
<td>0.5768(2)</td>
<td>0.2907(3)</td>
<td>0.071(3)</td>
</tr>
<tr>
<td>Mo2 (2i)</td>
<td>0.8221(6)</td>
<td>−0.0395(5)</td>
<td>0.2272(5)</td>
<td>0.071(3)</td>
</tr>
<tr>
<td>Fe (2i)</td>
<td>0.4001(4)</td>
<td>0.0996(4)</td>
<td>0.3175(2)</td>
<td>0.073(4)</td>
</tr>
<tr>
<td>Li (2i)</td>
<td>0.7580(2)</td>
<td>0.4418(2)</td>
<td>0.2557(2)</td>
<td>0.803(2)</td>
</tr>
<tr>
<td>O1 (2i)</td>
<td>0.4166(7)</td>
<td>0.8407(73)</td>
<td>0.3907(6)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O2 (2i)</td>
<td>0.2563(5)</td>
<td>0.5731(65)</td>
<td>0.0397(6)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O3 (2i)</td>
<td>0.0891(7)</td>
<td>0.4879(60)</td>
<td>0.3351(6)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O4 (2i)</td>
<td>0.4795(6)</td>
<td>0.3805(63)</td>
<td>0.3539(6)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O5 (2i)</td>
<td>0.6896(7)</td>
<td>0.1301(63)</td>
<td>0.2682(7)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O6 (2i)</td>
<td>0.7755(6)</td>
<td>−0.0499(70)</td>
<td>−0.0271(6)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O7 (2i)</td>
<td>0.7082(6)</td>
<td>−0.2787(60)</td>
<td>0.2690(9)</td>
<td>0.342(2)</td>
</tr>
<tr>
<td>O8 (2i)</td>
<td>1.1138(6)</td>
<td>0.0417(63)</td>
<td>0.3585(6)</td>
<td>0.342(2)</td>
</tr>
</tbody>
</table>

*Space group: P1̅, a = 6.751(1) Å, b = 7.203(2) Å, c = 7.1702(1) Å, α = 90.6739(17)°, β = 110.2274(14)°, γ = 105.5793(17)°, R_p = 3.00%, R_w = 5.61%.

The magnetic susceptibility (χ) and its inverse (1/χ) as a function of temperature (T) measured following zero field cooling (ZFC) and field cooling (FC) processes at 0.1 T field. The two curves almost overlap, and no bifurcation is seen in the whole temperature range, suggesting the absence of glass behavior. A peak of dχ/dT was observed around TN ~ 23.8 K, indicating the establishment of long-range magnetic ordering, as shown in the inset of Figure 2b. The χ(T) of LiFe(MoO4)2 can be well fitted to the Curie−Weiss law χ = C/(T − θCW), as also shown in Figure 2a. Our fitting in the temperature range between 100 and 300 K yields the Curie constant C ~ 4.53 emu K/mol and negative Curie−Weiss temperature θCW ~ −32.85 K, suggesting dominant AFM interactions between Fe’s spins. The effective moment per Fe3+ of 6.02 μB is very close to spin-only moment (5.92 μB) for high-spin Fe3+ (S = 5/2, L = 0).

Figure 2b shows the magnetic susceptibility under a high magnetic field (6 T). There is a maximum of γ at T_{max} ~ 32.8 K, which may due to the ordering of short-range magnetic
The obtained magnetic heat capacity

In addition, Figure 2c shows the magnetization (aforementioned long-range AFM magnetic ordering (LRO).

The broad hump in both magnetic susceptibility and specific heat around ∼10 K might originate from the temperature-dependent exchange effects. As suggested in ref 33, below $T_N$, the populations and energies of Zeeman levels due to the temperature-dependent exchange field would be more significant if the spin quantum number is large, as here the spin number $S = S/2$. The magnetic entropy ($S_M$) is estimated through integrating $C_M/T$ over $T$, giving a saturation value of $S_M \sim 11.9418 J/(mol K)$ at 80 K as shown in Figure 3b. This value is very close to the calculation value of total spin entropy of $R \ln(2S + 1) = 14.897 J/(mol K)$ ($R = 8.314 J/(mol K)$). The entropy gain at $T_N$ is only ∼48.8% of the total magnetic entropy, indicating the existence of short-range magnetic correlations above $T_N$, which is a characteristic of low-dimensional magnets.

To reveal the AFM spin structure of LiFe(MoO$_4$)$_2$, the NPD pattern was collected at 1.5 K. As shown in Figure 4b, a series of new Bragg peaks indicated by the second row of vertical bars show up compared to the data collected at 40 K. The inset displays a zoomed view of the low-Q region to show the peaks more clearly. No obvious change of lattice parameters was observed. In Figure 4c, the difference between the 40 and 1.5 K patterns clearly shows the details of these magnetic Bragg peaks. The observed magnetic peaks can be well indexed with a commensurate propagation vector $k = (0, 0.5, 0)$, distinct from the incommensurate one $k = (0.890, 0, 0.332)$ seen in LiFe(WO$_4$)$_2$ and a noncollinear triangular spin order seen in RbFe(MoO$_4$)$_2$.

Figure 4a exhibits the temperature evolution of the peak intensity of the $(0, 0, S, 1)$ magnetic Bragg peak. A fit to the power law $I = A(T_c - T)^\beta$ over the temperature range 8–29 K yields $T_c = 24.1(2) K$ and a critical exponent $\beta = 0.218$. The obtained $\beta$ is close to the expected value for the 2D-XY model (∼0.23) expected for layered magnetic structures.

Representation analysis constrains the possible magnetic structures to the basis vectors associated with an irreducible representation (IR) of the crystal space group and $k = (0, 0, S, 0)$. We used SARAh software to perform the analysis on magnetic Fe$^{3+}$ ions. There are two possible irreducible representation allowed for the Fe$^{3+}$ ion at the 2i Wyckoff position, corresponding to $\Gamma_1$ and $\Gamma_2$ in the Kovalev numbering scheme, as listed in Table 2. Three basis vectors are allowed for each representation. While the $\Gamma_1$ is ruled out since it cannot...
To reproduce the correct magnetic intensities, the $\Gamma_2$ spin model gives us good fitting results as shown in Figure 4b. The corresponding magnetic structure is presented in Figure 5 with the refined amplitude of the magnetic moment $4.23(1) \mu_B$. The projections of the moment on the crystallographic axes are $(m_{a}, m_{b}, m_{c}) = (0.582, 4.2, 1.296) \mu_B$. This value is only slightly smaller than the expected value for the spin $S = 5/2$, but it is still reasonable considering the low-dimensionality magnetic interactions.

To further understand the magnetic properties, DFT calculations have been performed. Various possible magnetic arrangements were checked, such as ferromagnetic (FM), AF1=AFM, AF2=AFM, and AF3=AFM, as shown in Figure 6. As shown in Figure 7, the AF2=AFM configuration has the lowest energy despite the choice of $U_{\text{eff}}$, in agreement with our neutron experimental result. The calculated local magnetic moment of the AF2=AFM state is $4.22 \mu_B/Fe$ at $U_{\text{eff}} = 4$ eV, which is quite close to our neutron experiments ($4.23 \mu_B/Fe$).

In fact, $U_{\text{eff}} = 4$ eV is a proper choice to describe Fe’s 3d orbitals according to previous studies, which will be adopted as the default one. The optimized lattice constants of the AF2=AFM state are $a = 6.748$ Å, $b = 7.233$ Å, and $c = 7.113$ Å, which are quite close to our neutron experiments ($a = 6.751$ Å, $b = 7.203$ Å, $c = 7.1702$ Å at 1.5 K).

Furthermore, the magnetism of LiFe(MoO₄)₂ can be described using a Heisenberg model:

$$ H = -J_1 \sum_{\langle ij \rangle} S_i \cdot S_j - J_2 \sum_{\langle k \rangle} S_k \cdot S_l - J_3 \sum_{\langle m n \rangle} S_m \cdot S_n $$

where $J_1$, $J_2$, and $J_3$ are the exchange couplings (as indicated in Figure 1b) between iron spins $S$s. Using the optimized ground state configuration, the exchange coefficients are extracted from DFT calculations: $J_1 = -18.03$ meV, $J_2 = 2.06$ meV, and $J_3 = 2.07$ meV, respectively. The strongest negative exchange $J_1$ indicates the AFM coupling between the nearest neighbor iron spins. Those longer distance exchanges $J_2$ and $J_3$ are much smaller.

As shown in Figure 7, the AF2=AFM configuration has the lowest energy despite the choice of $U_{\text{eff}}$, in agreement with our neutron experimental result. The calculated local magnetic moment of the AF2=AFM state is $4.22 \mu_B/Fe$ at $U_{\text{eff}} = 4$ eV, which is quite close to our neutron experiments ($4.23 \mu_B/Fe$).
weaker: the positive $J_1$ implies FM interaction along the $b$-axis, and the positive $J_3$ means that the magnetic coupling between near iron is FM exchange. In short, our theoretical calculation confirms the magnetic ground state of LiFe(MoO$_4$)$_2$.

The atomic-projected density of states (DOS) of the AF2–AFM state is shown in Figure 8. It is clear that this system is an insulator with an indirect gap of 2.46 eV. According to DOS, the topmost valence bands are mainly contributed by the hybrid O’s 3p orbitals and Fe’s 3d orbitals (lower Hubbard bands), while the lowest conduction bands are mainly from Fe’s 3d orbitals (i.e., upper Hubbard bands). The slight reduction of local magnetic moment from the ideal 5 $\mu_B$/Fe is due to such hybridization.

**IV. CONCLUSION**

In summary, the physical properties of the spin-5/2 double molybdate LiFe(MoO$_4$)$_2$ have been systematically investigated experimentally and theoretically. Our magnetic susceptibility and heat capacity measurements found an antiferromagnetic long-range ordering at $T_N \sim 23.8$ K, which was further confirmed by neutron diffraction. Its antiferromagnetic magnetic structure with the commensurate propagation vector $k = (0, 0.5, 0)$ has also been determined. Our DFT calculations further verified the magnetic ground state. Short-range magnetic correlation was also made evident above the Néel temperature.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.inorgchem.0c00432.

Powder diffraction data table (PDF)

Magnetic structure file of LiFe(MoO$_4$)$_2$ (MCIF)

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**Notes**

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